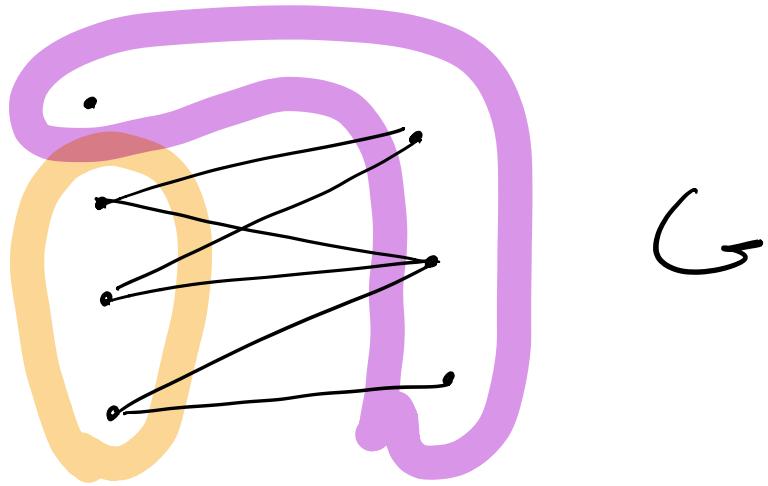


Def G is bipartite if we can find $P_1, P_2 \subset V(G)$

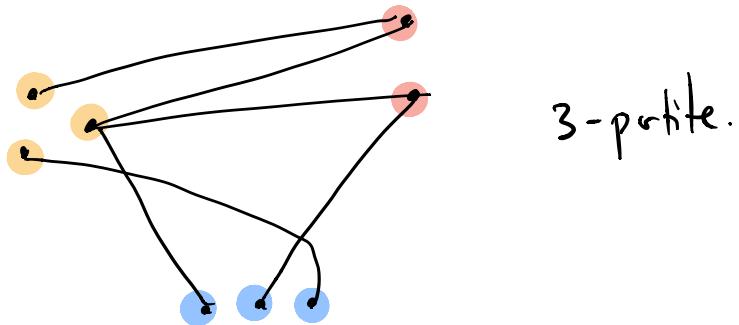
$$\text{s.t. } P_1 \cup P_2 = V(G) \quad P_1 \cap P_2 = \emptyset$$

if $v, w \in P_i, i=1 \text{ or } 2$ then $v \notin w$ are not adjacent.



Def We say G is k -partite, if we can find $P_1, P_2, \dots, P_k \subset V(G)$ s.t $\bigcup_{i=1}^k P_i = V(G)$ &

$P_i \cap P_j = \emptyset$ all $i \neq j$. such that $u, w \in P_i$
then u, w are not adjacent.

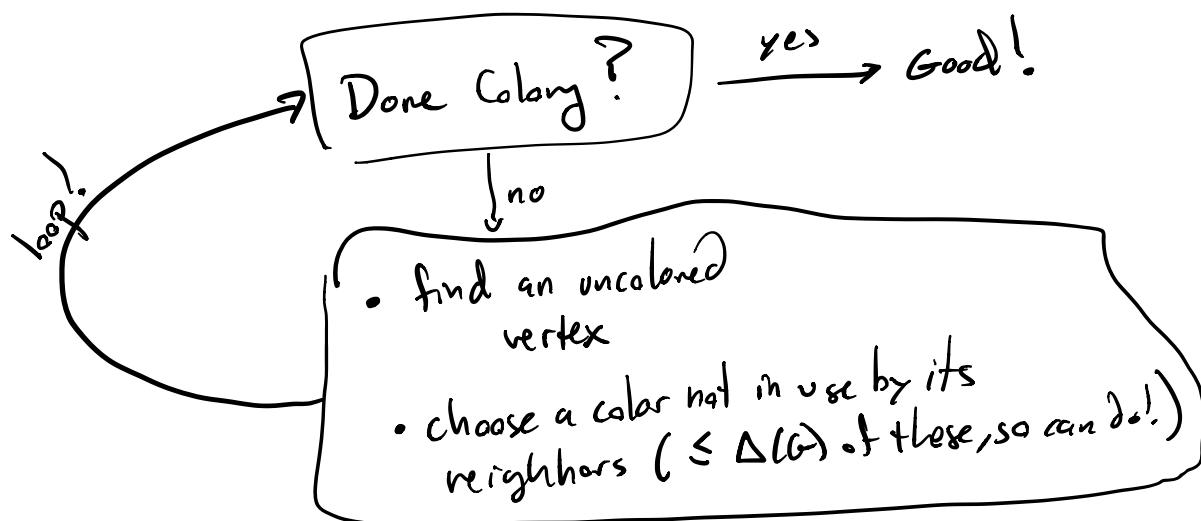


Observation

G is k -colorable $\Leftrightarrow G$ is k -partite.

How to color a graph?

Naive Algorithm: (Conclusion, can use at most $\Delta(G) + 1$ colors)



Smarter Algorithm

